22. Calculate first four moments about the mean from the following data:

Mark: 0-10 10-20 20-30 30-40 40-50 50-60 60-70 No. of students: 8 12 20 30 15 10 5

- 23. An urn X contains 3 white and 5 black balls. Another urn Y contains 6 white and 4 black balls. A ball is transferred from the Urn X to urn Y, then a ball is taken from urn Y. Find the probability that it will be white.
- 24. The following data represents the number of units of commodity produced by 3 different workers using 3 different types of machines.

Vorkers	Ma	Machines		
S.,	A	В	C	
X	16	64	40	
Y	56	72	56	
Z	12	56	28	

Test (a) whether the mean productivity is the same for the different machine types, and (b) whether the three workers differ with respect to mean productivity.

Time: Three hours

Maximum: 75 marks

PART A — $(10 \times 2 = 20 \text{ marks})$

Answer any TEN questions.

- List the rules to round-off a number.
- 2. What is Gauss elimination method?
- 3. State trapezoidal rule to evaluate $\int_{a}^{b} f(x)dx$.
- 4. Write Runge-Kutta second order formula to solve $\frac{dy}{dx} = f(x, y), \ y(x_0) = y_0.$
- 5. Find the geometric mean of 2,8, 18, and 72.
- 6. Define Range and standard deviation.
- 7. Define Conditional probability.
- 8. Find the mathematical expectation of tails appearing in tossing two coins.

- 9. Write the normal equations to fit a curve of the form $y = ax^2 + bx + c$.
- 10. State any two properties of multiple correlation.
- 11. Write recursive formula to find a solution of f(x)=0 using secant method.
- 12. Write the mean and variance of Poisson distribution.

PART B — $(5 \times 5 = 25 \text{ marks})$

Answer any FIVE questions.

- 13. Find the root of the equation $y(x) = x^3 2x 5 = 0$, which lies between 2 and 3 using Muller method.
- 14. Evaluate $\int_{4}^{5.2} f(x)dx$ by (a) Trapezoidal method and

(b) Simpson's 1/3rd rule for the following data: x: 4 4.2 4.4 4.6 4.8 5.0 5.2

f(x): 1.3862 1.4351 1.4816 1.5261 1.5686 1.6094 1.6486

15. Find the mean deviation about median for the following data:

Class: 0-10 10-20 20-30 30-40 40-50 50-60 60-70 70-80 Frequency: 5 8 12 15 20 14 12 6

- 16. A problem in Statistics is given to five students A, B, C, D and E. Their chances of solving it are $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$, $\frac{1}{5}$ and $\frac{1}{6}$. What is the probability that the problem will be solved?
- 17. From the following data obtain the regression equation of y on x.

X: 6 2 10 4 8

Y: 9 11 5 8 7

- 18. Find a positive root of the equation $xe^x = 2$ which lies between 0 and 1 by Regula-Falsi method.
- 19. In a trivariate distribution $\sigma_1=2$, $\sigma_2=\sigma_3=3$, $r_{12}=0.7$, $r_{23}=r_{31}=0.5$. Find $b_{12,3}$.

PART C — $(3 \times 10 = 30 \text{ marks})$

Answer any THREE questions.

20. Use Gauss-Jordan method to solve the following system of equations:

$$10x + y + z = 12$$
, $2x + 10y + z = 13$, $x + y + 5z = 7$

21. Use Taylor's series compute y(0.2), y(0.4) given $\frac{dy}{dx} = 1 - 2xy$, y(0) = 0.